### MATH 5 Course Outline as of Summer 2019

### **CATALOG INFORMATION**

Title: INTRO TO LINEAR ALGEBRA Dept and Nbr: MATH 5

Full Title: Introduction to Linear Algebra

Last Reviewed: 2/8/2021

Units		Course Hours per Week		Nbr of Weeks	<b>Course Hours Total</b>	
Maximum	3.00	Lecture Scheduled	3.00	17.5	Lecture Scheduled	52.50
Minimum	3.00	Lab Scheduled	0	17.5	Lab Scheduled	0
		Contact DHR	0		Contact DHR	0
		Contact Total	3.00		Contact Total	52.50
		Non-contact DHR	0		Non-contact DHR	0

Total Out of Class Hours: 105.00 Total Student Learning Hours: 157.50

Title 5 Category: AA Degree Applicable

Grading: **Grade Only** 

00 - Two Repeats if Grade was D, F, NC, or NP Repeatability:

Also Listed As:

Formerly:

### **Catalog Description:**

An introduction to linear algebra including the theory of matrices, determinants, vector spaces, linear transformations, eigenvectors, eigenvalues and applications.

### **Prerequisites/Corequisites:**

Completion of MATH 1B or higher (MATH)

### **Recommended Preparation:**

Concurrent enrollment in MATH 1C or MATH 2

#### **Limits on Enrollment:**

#### **Schedule of Classes Information:**

Description: An introduction to linear algebra including the theory of matrices, determinants, vector spaces, linear transformations, eigenvectors, eigenvalues and applications. (Grade Only) Prerequisites/Corequisites: Completion of MATH 1B or higher (MATH)

Recommended: Concurrent enrollment in MATH 1C or MATH 2

Limits on Enrollment: Transfer Credit: CSU;UC.

Repeatability: Two Repeats if Grade was D, F, NC, or NP

# **ARTICULATION, MAJOR, and CERTIFICATION INFORMATION:**

AS Degree: Area Effective: Inactive: CSU GE: Transfer Area Effective: Inactive:

**IGETC:** Transfer Area Effective: Inactive:

**CSU Transfer:** Transferable Effective: Spring 1989 Inactive:

**UC Transfer:** Transferable Effective: Spring 1989 Inactive:

CID:

CID Descriptor:MATH 250 Introduction to Linear Algebra

SRJC Equivalent Course(s): MATH5

### **Certificate/Major Applicable:**

Major Applicable Course

# **COURSE CONTENT**

### **Student Learning Outcomes:**

At the conclusion of this course, the student should be able to:

- 1. Determine the dimensions of a variety of vector spaces.
- 2. Find eigenvalues, eigenvectors and eigenspaces of matrices and linear transformations.
- 3. Determine matrix representations of linear transformations and linear operators.

### **Objectives:**

Upon successful completion of the course, students will be able to:

- 1. Solve systems of linear equations using Gauss-Jordan elimination, matrix inverses and Cramer's rule.
- 2. Define operations on matrices, invertibility, elementary matrices, orthogonal matrices.
- 3. Use properties of determinants including row reduction to evaluate determinants.
- 4. Invert matrices using adjoints and cofactors.
- 5. Define vector spaces, subspaces, span, linear independence, bases, dimension, inner product spaces, and orthonormal bases.
- 6. Determine the nullspace or kernel and range of a matrix and linear transformation.
- 7. Determine the injectivity and surjectivity of linear transformations and linear operators.
- 8. Define and determine dimension, rank and nullity of a matrix.
- 9. Determine the matrix representation of a linear transformation using different bases and using change of basis.
- 10.Determine eigenvalues, eigenvectors and eigenspaces of matrices and linear transformations.
- 11. Apply proof writing techniques to prove basic results in linear algebra.

### **Topics and Scope:**

- I. Vectors
  - A. Review of vectors in 2- and 3-dimensional real space
  - B. Vectors in n-dimensional real space
  - C. Properties of vectors in n-dimensional real space, including dot product, norm of a vector, angle between vectors, & vector orthogonality

## II. Matrices

- A. Systems of linear equations
- B. Gauss-Jordan elimination
- C. Operations on matrices, including the transpose
- D. Invertibility
- E. Triangular matrices
- F. Elementary matrices
- G. Orthogonal matrices

### III. Determinants

- A. Properties
- B. Evaluation by row reduction
- C. Cofactors and adjoints
- D. Formula for inverse of a matrix
- E. Cramer's rule

### IV. Real Vector Spaces

- A. Defining properties
- B. Subspace
- C. Span
- D. Linear independence
- E. Basis
- F. Dimension
- G. Rank
- H. Solution space of a system of linear equations
- I. Inner product spaces
- J. Orthonormal bases
- K. Gram-Schmidt process

# V. Linear Transformations

- A. Kernel
- B. Range
- C. Rank and nullity
- D. Matrix representation of linear transformation
- E. Similarity
- F. Change of basis
- G. One-to-one and onto

### VI. Eigenvectors and Eigenvalues

- A. Characteristic equations
- B. Eigenspaces
  - 1. Diagonalization of matrices
  - 2. Orthogonal diagonalization of symmetric matrices

### VII. Proofs applied to:

- A. Linear independence of vectors
- B. Properties of subspaces
- C. Linearity, subjectivity & surjectivity of functions
- D. Properties of Eigenvectors and Eigenvalues

### VIII. Applications may include:

- A. Differential equations
- B. Fourier series
- C. Quadratic forms
- D. Gauss-Seidel method
- E. Partial pivoting
- F. Eigenvalues, Eigenvalue approximations & Eigenvectors

### **Assignment:**

- 1. Reading outside of class (0-50 pages per week)
- 2. Problem sets (15-30)
- 3. Midterm exams (2-5), quizzes (0-20) and final exam

#### Methods of Evaluation/Basis of Grade:

**Writing:** Assessment tools that demonstrate writing skills and/or require students to select, organize and explain ideas in writing.

None, This is a degree applicable course but assessment tools based on writing are not included because problem solving assessments are more appropriate for this course.

Writing 0 - 0%

**Problem Solving:** Assessment tools, other than exams, that demonstrate competence in computational or non-computational problem solving skills.

Problem sets

Problem solving 5 - 20%

**Skill Demonstrations:** All skill-based and physical demonstrations used for assessment purposes including skill performance exams.

None

Skill Demonstrations 0 - 0%

**Exams:** All forms of formal testing, other than skill performance exams.

Exams and quizzes (free response, multiple choice, true/false)

Exams 80 - 95%

**Other:** Includes any assessment tools that do not logically fit into the above categories.

None

Other Category 0 - 0%

# Representative Textbooks and Materials:

Elementary Linear Algebra (11th). Anton, Howard. Wiley: 2014

Linear Algebra and Its Applications (4th). Lay, David C. Pearson: 2012