## CATALOG INFORMATION

Dept and Nbr: MATH 74 Title: NUMBER SYSTEMS
Full Title: Mathematics for Elementary School Teachers - Number Systems
Last Reviewed: 1/9/2024

| Units |  | Course Hours per W |  | Nbr of Weeks | Course Hours Total |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Maximum | 4.00 | Lecture Scheduled | 4.00 | 17.5 | Lecture Scheduled | 70.00 |
| Minimum | 4.00 | Lab Scheduled | 0 | 6.5 | Lab Scheduled | 0 |
|  |  | Contact DHR | 0 |  | Contact DHR | 0 |
|  |  | Contact Total | 4.00 |  | Contact Total | 70.00 |

Non-contact DHR 0
Non-contact DHR
0

Total Out of Class Hours: 140.00
Total Student Learning Hours: 210.00

Title 5 Category: AA Degree Applicable
Grading: Grade Only
Repeatability: $\quad 00$ - Two Repeats if Grade was D, F, NC, or NP
Also Listed As:
Formerly:

## Catalog Description:

Students will learn mathematical concepts needed for teaching elementary school mathematics including quantitative reasoning, number systems and subsystems, basic number theory, logical thinking, and applications. Content is relevant to national curriculum standards and Common Core State Standards.

## Prerequisites/Corequisites:

Completion of MATH 161 or MATH 154 or MATH 156 or AB705 placement into <a href='https://assessment.santarosa.edu/understanding-your-math-placement'
class='NormalSiteLink' target='_New'>Math Tier 2 or higher</a>

## Recommended Preparation:

## Limits on Enrollment:

## Schedule of Classes Information:

Description: Students will learn mathematical concepts needed for teaching elementary school mathematics including quantitative reasoning, number systems and subsystems, basic number theory, logical thinking, and applications. Content is relevant to national curriculum standards
and Common Core State Standards. (Grade Only)
Prerequisites/Corequisites: Completion of MATH 161 or MATH 154 or MATH 156 or AB705
placement into <a href='https://assessment.santarosa.edu/understanding-your-math-placement' class='NormalSiteLink' target='_New'>Math Tier 2 or higher</a>
Recommended:
Limits on Enrollment:
Transfer Credit: CSU;
Repeatability: Two Repeats if Grade was D, F, NC, or NP

## ARTICULATION, MAJOR, and CERTIFICATION INFORMATION:

| AS Degree: | Area B <br> MC | Communication and Analytical <br> Thinking <br> Math Competency |  | Effective: <br> Fall 2023 | Inactive: |
| :---: | :---: | :---: | :---: | :---: | :---: |
| CSU GE: | Transfer Area B4 | Math/Qua | ive Reasoning | Effective: <br> Fall 2024 | Inactive: |
| IGETC: | Transfer Area |  |  | Effective: | Inactive: |
| CSU Transfer | :Transferable | Effective: | Fall 2023 | Inactive: |  |
| UC Transfer: |  | Effective: |  | Inactive: |  |
| CID: |  |  |  |  |  |
| Certificate/M <br> Both Certificat | ajor Applicable: and Major App | plicable |  |  |  |

## COURSE CONTENT

## Student Learning Outcomes:

At the conclusion of this course, the student should be able to:

1. Analyze the structure and properties of different number systems including real numbers and their subsystems.
2. Use basic number theory including divisibility tests, prime and composite numbers, and the Fundamental Theorem of Arithmetic.
3. Develop and reinforce conceptual understanding of mathematical topics through the use of patterns, problem solving, communication, connections, modeling, reasoning, and representation.
4. Explain national and state standards for elementary school curriculum, including Common Core.

## Objectives:

At the conclusion of this course, the student should be able to:

1. Perform calculations with place value systems including base ten and other natural number bases.
2. Apply concepts and algorithms from number theory to determine divisibility, least common multiple or greatest common divisor for positive integers and solve related application problems.
3. Understand the implications of the Fundamental Theorem of Arithmetic.
4. Expound on the concept of rational numbers by illustrating them through both ratio and
decimal representations.
5. Describe the arithmetic algorithms for operations on rational numbers.
6. Describe the structure and properties of integers, rational numbers, and real numbers.
7. Develop, model, and solve problems using reasoning, logic, and pattern recognition.
8. Develop activities implementing curriculum standards.
9. Utilize sets, functions, patterns, connections, modeling, as well as deductive or inductive reasoning as a collective toolkit for problem-solving.
10. Prove mathematical statements involving positive integers by using the Principle of Mathematical Induction.

## Topics and Scope:

I. Numeration Systems
A. Historical
B. Hindu-Arabic
C. Place-value

1. Base 10
2. Other bases
II. Basic Number Theory
A. Divisibility
B. Prime and composite numbers
C. Prime factorization
D. Fundamental Theorem of Arithmetic
E. Least common multiple
F. Greatest common divisor
III. Integers
A. Structure
B. Properties
C. Computational algorithms
IV. Rational Numbers
A. Structure
B. Properties
C. Computational algorithms
D. Ratio and proportion
E. Decimal representation
V. Real Numbers
A. Structure
B. Properties
C. Irrational numbers
D. Decimal representation
E. Number line representation
VI. Conceptual Understanding
A. Patterns
B. Problem solving
C. Reasoning
D. Modeling
VII. National and State Standards

## A. Process standards

1. Problem-solving
2. Reasoning
3. Communication
4. Representation
5. Connection
B. Mathematical proficiency
6. Adaptive reasoning
7. Strategic competence
8. Conceptual understanding
9. Procedural fluency
10. Productive disposition

## Assignment:

1. Reading outside of class ( $0-60$ pages per week)
2. Problem set(s) (1-8 per week)
3. Quiz(zes) ( $0-4$ per week)
4. Project(s) (0-10)
5. Exams (2-6)
6. Final exam

## Methods of Evaluation/Basis of Grade:

Writing: Assessment tools that demonstrate writing skills and/or require students to select, organize and explain ideas in writing.

None, This is a degree applicable course but assessment tools based on writing are not included because problem solving assessments are more appropriate for this course.

Writing
0-0\%

Problem Solving: Assessment tools, other than exams, that demonstrate competence in computational or noncomputational problem solving skills.

## Problem set(s)

Problem solving
5-20\%
Skill Demonstrations: All skill-based and physical demonstrations used for assessment purposes including skill performance exams.

None
Exams: All forms of formal testing, other than skill performance exams.

Quiz(zes); exams; final exam


Other: Includes any assessment tools that do not logically fit into the above categories.

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Project(s)
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Representative Textbooks and Materials:
A Problem Solving Approach to Mathematics for Elementary School Teachers. 13th ed.

Billstein, R., Libeskind, S., and Lott, J.W. Pearson. 2020.
Mathematical Reasoning for Elementary Teachers. 7th ed. Long, C., De Temple, D., and Millman R. Pearson. 2019.

