### MATH 74 Course Outline as of Fall 2024

# **CATALOG INFORMATION**

Dept and Nbr: MATH 74 Title: NUMBER SYSTEMS Full Title: Mathematics for Elementary School Teachers - Number Systems Last Reviewed: 1/9/2024

Units		Course Hours per Week		Nbr of Weeks	<b>Course Hours Total</b>	
Maximum	4.00	Lecture Scheduled	4.00	17.5	Lecture Scheduled	70.00
Minimum	4.00	Lab Scheduled	0	6.5	Lab Scheduled	0
		Contact DHR	0		Contact DHR	0
		Contact Total	4.00		Contact Total	70.00
		Non-contact DHR	0		Non-contact DHR	0

Total Out of Class Hours: 140.00

Total Student Learning Hours: 210.00

Title 5 Category:	AA Degree Applicable
Grading:	Grade Only
Repeatability:	00 - Two Repeats if Grade was D, F, NC, or NP
Also Listed As:	
Formerly:	

#### **Catalog Description:**

Students will learn mathematical concepts needed for teaching elementary school mathematics including quantitative reasoning, number systems and subsystems, basic number theory, logical thinking, and applications. Content is relevant to national curriculum standards and Common Core State Standards.

#### **Prerequisites/Corequisites:**

Completion of MATH 161 or MATH 154 or MATH 156 or AB705 placement into <a href='https://assessment.santarosa.edu/understanding-your-math-placement' class='NormalSiteLink' target='\_New'>Math Tier 2 or higher</a>

### **Recommended Preparation:**

### **Limits on Enrollment:**

# Schedule of Classes Information:

Description: Students will learn mathematical concepts needed for teaching elementary school mathematics including quantitative reasoning, number systems and subsystems, basic number theory, logical thinking, and applications. Content is relevant to national curriculum standards

and Common Core State Standards. (Grade Only) Prerequisites/Corequisites: Completion of MATH 161 or MATH 154 or MATH 156 or AB705 placement into <a href='https://assessment.santarosa.edu/understanding-your-math-placement' class='NormalSiteLink' target='\_New'>Math Tier 2 or higher</a> Recommended: Limits on Enrollment: Transfer Credit: CSU; Repeatability: Two Repeats if Grade was D, F, NC, or NP

# **ARTICULATION, MAJOR, and CERTIFICATION INFORMATION:**

AS Degree:	Area B	Communication and Analytical Thinking Math Competency Math/Quantitative Reasoning		Effective: Fall 2023	Inactive:
CSU GE:	MC <b>Transfer Area</b> B4			Effective: Fall 2024	Inactive:
<b>IGETC:</b>	Transfer Area			Effective:	Inactive:
CSU Transfer	: Transferable	Effective:	Fall 2023	Inactive:	
UC Transfer:		Effective:		Inactive:	

### CID:

### **Certificate/Major Applicable:**

Both Certificate and Major Applicable

# **COURSE CONTENT**

# **Student Learning Outcomes:**

At the conclusion of this course, the student should be able to:

1. Analyze the structure and properties of different number systems including real numbers and their subsystems.

2. Use basic number theory including divisibility tests, prime and composite numbers, and the Fundamental Theorem of Arithmetic.

3. Develop and reinforce conceptual understanding of mathematical topics through the use of patterns, problem solving, communication, connections, modeling, reasoning, and representation.

4. Explain national and state standards for elementary school curriculum, including Common Core.

# **Objectives:**

At the conclusion of this course, the student should be able to:

1. Perform calculations with place value systems including base ten and other natural number bases.

2. Apply concepts and algorithms from number theory to determine divisibility, least common multiple or greatest common divisor for positive integers and solve related application problems.

3. Understand the implications of the Fundamental Theorem of Arithmetic.

4. Expound on the concept of rational numbers by illustrating them through both ratio and

decimal representations.

- 5. Describe the arithmetic algorithms for operations on rational numbers.
- 6. Describe the structure and properties of integers, rational numbers, and real numbers.
- 7. Develop, model, and solve problems using reasoning, logic, and pattern recognition.
- 8. Develop activities implementing curriculum standards.

9. Utilize sets, functions, patterns, connections, modeling, as well as deductive or inductive reasoning as a collective toolkit for problem-solving.

10. Prove mathematical statements involving positive integers by using the Principle of Mathematical Induction.

# **Topics and Scope:**

- I. Numeration Systems
  - A. Historical
  - B. Hindu-Arabic
  - C. Place-value
    - 1. Base 10
    - 2. Other bases
- II. Basic Number Theory
  - A. Divisibility
  - B. Prime and composite numbers
  - C. Prime factorization
  - D. Fundamental Theorem of Arithmetic
  - E. Least common multiple
  - F. Greatest common divisor
- III. Integers
  - A. Structure
  - B. Properties
  - C. Computational algorithms
- IV. Rational Numbers
  - A. Structure
  - **B.** Properties
  - C. Computational algorithms
  - D. Ratio and proportion
  - E. Decimal representation
- V. Real Numbers
  - A. Structure
  - **B.** Properties
  - C. Irrational numbers
  - D. Decimal representation
  - E. Number line representation
- VI. Conceptual Understanding
  - A. Patterns
  - B. Problem solving
  - C. Reasoning
  - D. Modeling
- VII. National and State Standards
  - A. Process standards
    - 1. Problem-solving
    - 2. Reasoning
    - 3. Communication
    - 4. Representation

- 5. Connection
- B. Mathematical proficiency
  - 1. Adaptive reasoning
  - 2. Strategic competence
  - 3. Conceptual understanding
  - 4. Procedural fluency
  - 5. Productive disposition

#### Assignment:

- 1. Reading outside of class (0-60 pages per week)
- 2. Problem set(s) (1-8 per week)
- 3. Quiz(zes) (0-4 per week)
- 4. Project(s) (0-10)
- 5. Exams (2-6)
- 6. Final exam

### Methods of Evaluation/Basis of Grade:

**Writing:** Assessment tools that demonstrate writing skills and/or require students to select, organize and explain ideas in writing.

None, This is a degree applicable course but assessment tools based on writing are not included because problem solving assessments are more appropriate for this course.

**Problem Solving:** Assessment tools, other than exams, that demonstrate competence in computational or non-computational problem solving skills.

Problem set(s)

**Skill Demonstrations:** All skill-based and physical demonstrations used for assessment purposes including skill performance exams.

None

**Exams:** All forms of formal testing, other than skill performance exams.

Quiz(zes); exams; final exam

**Other:** Includes any assessment tools that do not logically fit into the above categories.

Project(s)

# **Representative Textbooks and Materials:**

A Problem Solving Approach to Mathematics for Elementary School Teachers. 13th ed.

Writing 0 - 0%

Problem solving

5 - 20%

Skill Demonstrations 0 - 0%

> Exams 70 - 95%

Other Category	
0 - 20%	

Billstein, R., Libeskind, S., and Lott, J.W. Pearson. 2020. Mathematical Reasoning for Elementary Teachers. 7th ed. Long, C., De Temple, D., and Millman R. Pearson. 2019.